Ma

KEY STAGE

16VELS 3–5 2006

Mathematics tests Mark schemes

Test A, test B and mental mathematics test



department for education and skills

creating opportunity, releasing potential, achieving excellence

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Marking the mathematics tests

As in 2005, external markers, employed by the external marking agencies under contract to QCA, will mark the test papers. The markers will follow the mark schemes in this booklet, which is supplied to teachers for information.

This booklet contains the mark schemes for the levels 3–5 tests A, B and mental mathematics. Level threshold tables will be available on the QCA website on 19 June 2006 (www.qca.org.uk).

General guidance

The structure of the mark schemes

The marking information for each question is set out in the form of tables, which start on page 6 of this booklet. The '**question**' column on the left-hand side of each table provides a quick reference to the question number and the question part. The '**mark**' column indicates the total number of marks available for each question part. On some occasions the symbol \bigcirc may be shown in the mark column. The 'U' indicates that there is a *Using and applying mathematics* element in the question. The number, 1, shows the number of marks attributed to using and applying mathematics in this question.

The 'requirement' column may include two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working
- examples of some different types of correct response.

The 'additional guidance' column indicates alternative acceptable responses, and provides details of specific types of response which are unacceptable. Other guidance, such as the range of acceptable answers, is provided as necessary.

Additionally, for the mental mathematics test, general guidance on marking is given on page 18, together with a 'quick reference' mark scheme.

Applying the mark schemes

In order to ensure consistency of marking, the most frequent procedural queries are listed on pages 2 and 3 with the action the marker will take. This is followed by further guidance on pages 4 and 5 relating to the marking of questions that involve money, time and other measures. Unless otherwise specified in the mark scheme, markers will apply the following guidelines in all cases.

What if	Marking procedure		
The pupil's response is numerically or algebraically equivalent to the answer in the mark scheme.	Markers will award the mark unless the mark scheme states otherwise.		
The pupil's response does not match closely any of the examples given.	Markers will use their judgement in deciding whether the statement of the requirements given in the fractional guidance and, if also be made to the additional guidance and, if contact the supervising marker.	requirement' column. Reference will	
The pupil has responded in a non-standard way.	Calculations, formulae and written responses do not have to be set out in any particular format. Pupils may provide evidence in any form as long as its meaning can be understood. Diagrams, symbols or words are acceptable for explanations or for indicating a response. Any correct method of setting out working, however idiosyncratic, will be accepted.		
There appears to be a misreading affecting the working.	This is when the pupil misreads the information given in the question and uses different information without altering the original intention or difficulty level of the question. For each misread that occurs, one mark only will be deducted. In one-mark questions – 0 marks are awarded. In two-mark questions that have a method mark – 1 mark will be awarded if the correct method is correctly implemented with the misread number.		
No answer is given in the expected place, but the correct answer is given elsewhere.	Where a pupil has shown understanding of the question, the mark(s) will be given. In particular, where a word or number response is expected, a pupil may meet the requirement by annotating a graph or labelling a diagram elsewhere in the question.		
The response in the answer box is wrong, but the correct answer is shown in the working.	 Where appropriate, detailed guidance will be given in the mark scheme, which markers will follow. If no guidance is given, markers will examine each case to decide whether: the incorrect answer is due to a transcription error the pupil has continued to give redundant extra working which does not contradict work already done the pupil has continued to give redundant extra working which does contradict work already done. 	If so, the mark will be awarded. If so, the mark will be awarded. If so, the mark will not be awarded.	

What if	Marking procedure
The pupil's answer is correct but the wrong working is shown.	A correct response will always be marked as correct.
The correct response has been crossed out and not replaced.	Any legible crossed-out work that has not been replaced will be marked according to the mark scheme. If the work is replaced, then crossed-out work will not be considered.
More than one answer is given.	If all answers are correct (or a range of answers is given, all of which are correct), the mark will be awarded unless prohibited by the mark scheme. If both correct and incorrect responses are given, no mark will be awarded.
The answer is correct but, in a later part of the question, the pupil has contradicted this response.	A mark given for one part will not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise.
The pupil has drawn lines which do not meet at the correct point.	Markers will interpret the phrase 'slight inaccuracies in drawing' to mean 'within or on a circle of radius 2mm with centre at the correct point'.

Recording marks awarded on the test paper

All questions, even those not attempted by the pupil, will be marked with a '1' or '0' entered in each marking space.

A two-mark question which is correct will have '1' entered in both marking spaces. A two-mark question which is incorrect, but which has sufficient evidence of working or method as required by the mark scheme, will have '1' entered in the first marking space and '0' in the second. Otherwise '0' will be entered in both marking spaces.

For the written tests, the total number of marks gained on each double page will be written in the space at the bottom of the right-hand page. For all of the tests, the total number of marks gained on each paper will be recorded on the front of the test paper, and on the mark sheet.

Test A carries a total of 40 marks. Test B also carries a total of 40 marks. The mental mathematics test carries a total of 20 marks.

The 2006 key stage 2 mathematics tests and mark schemes were developed by the Mathematics Test Development Team at Edexcel.

Marking specific types of question – summary of additional guidance

Responses involving money

	Accept	Do not accept
Where the £ sign is given for example: £3.20, £7 £	£3.20£7 £7.00Any unambiguous indication of the correct amount, eg£3.20p£3 20 pence£3 20£3.20£3.20£3.20£3.20£3.20£3.20£3.20	Incorrect placement of pounds or pence, eg £320 £320p Incorrect placement of decimal point, or incorrect use or omission of 0, eg £3.2 £3 200 £32 0 £3-2-0
Where the p sign is given for example: 40p p	40p Any unambiguous indication of the correct amount, eg £0.40p	Incorrect or ambiguous use of pounds or pence, eg 0.40p £40p
Where no sign is given for example: £3.20, 40p	£3.2040p320p£0.40Any unambiguous indication of the correct amount, eg£3.20p£0.40p£3.20pence£.40p£3.20£.40£3.200.40£3.200.40£3.203.203.203.203 pounds 20	Incorrect or ambiguous use of pounds or pence, eg f320 £40 f320p £40p f3.2 0.4 3.20p

Responses involving time

	Accept	Do not accept
A time interval for example: 2 hours 30 minutes	2 hours 30 minutes Any unambiguous, correct indication, eg 2 ¹ / ₂ hours 2.5 hours 2h 30 2h 30min 150 minutes 150 Digital electronic time, ie 2:30	Incorrect or ambiguous time interval, eg 2.30 2-30 2,30 2.3 2.3 2.3 hours 2.3h 2h 3 2.30 min
A specific time for example: 8:40am, 17:20	8:40am 8:40 twenty to nine Any unambiguous, correct indication, eg 08.40 8.40 0840 8 40 8-40 8,40 Unambiguous change to 12 or 24 hour clock, eg 17:20 as 5:20pm or 17:20pm	Incorrect time, eg 8.4am 8.40pm Incorrect placement of separators, spaces etc or incorrect use or omission of 0, eg 840 8:4:0 8.4 084 84

Responses involving measures

	Accept	Do not accept
Where units are given (eg kg, m, l) for example: 8.6kg kg	8.6kgAny unambiguous indication of the correct measurement, eg8.60kg8.6000kg8kg 600g	Incorrect or ambiguous use of units, eg 8600kg

Note

If a pupil leaves the answer box empty but writes the answer elsewhere on the page, then that answer must be consistent with the units given in the answer box and the conditions listed above.

If a pupil changes the unit given in the answer box, then their answer must be equivalent to the correct answer using the unit they have chosen, unless otherwise indicated in the mark scheme.

Test A questions 1–3

Question	Requirement	Mark	Additional guidance
1	Numbers written in correct order as shown: 109 190 901 910 1091	1m	
2	One line of symmetry correctly positioned on each diagram as shown:	1m	Accept slight inaccuracies in drawing provided the intention is clear. The length of the line is unimportant provided the intention is clear.
За	Graph completed as shown:	1m	Accept bar for 'blue tit' in the range 2.5 to 3.5 exclusive. Accept bar for 'other' within 2mm of correct length.
3b	<u>1</u>	1m	Accept equivalent fractions, eg $\frac{5}{20}$ Do not accept 5

Test A questions 4–8

Question	Requirement	Mark	Additional guidance
4a	4	1m	
4b	150	1m	
5	Diagram completed as shown: 20 30 -70	1m	
6a	1 hour 20 minutes	1m	The answer is a time interval (see page 5 for guidance).
6b	3:25	1m	The answer is a specific time (see page 5 for guidance).
7a	Boxes ticked as shown:	1m (U1)	Accept alternative unambiguous indications such as Y or N .
7b	Boxes ticked as shown:	1m (U1)	Accept alternative unambiguous indications such as Y or N .
8a	451	1m	
8b	110	1m	

Test A questions 9–13

Question	Requirement	Mark	Additional guidance
9	Award TWO marks for the correct answer of 5 If the answer is incorrect, award ONE mark for evidence of appropriate working, eg $5 \times 25 = 125$ $12 \times 10 = 120$ 125 - 120 = wrong answer	Up to 2m	Calculation must be performed for the award of ONE mark.
10	1717	1m	
11 12a 12b	All numbers matched correctly as shown: 0.25 0.4 0.4 2 10 0.75 1 4 4 Monday AND Thursday	1m 1m 1m	 Do not award the mark if additional incorrect lines are drawn. Lines need not touch the numbers provided the intention is clear. Do not accept a list of days of the week. Accept unambiguous abbreviations or recognisable misspellings.
			Accept days written in either order.
13	Award TWO marks for numbers written in the correct regions as shown: $ \frac{factors of 30}{5} \frac{factors of 40}{7} $ If the answer is incorrect, award ONE mark for any three numbers written in the correct regions.	Up to 2m	Do not accept numbers written in more than one region. Accept alternative indications such as lines drawn from the numbers to the appropriate regions of the diagram.

Question	Requirement	Mark	Additional guidance
	1876 telephone 1800 2000 1810 1945 1810 1945 tin can 1945		Lines need not touch the time line provided the intended accuracy is clear.
14a	Answer for tin can joined to the time line in the range 1805 to 1815 exclusive.	1m	
14b	Answer for computer joined to the time line in the range 1940 to 1950 exclusive.	1m	
15a	Two numbers circled as shown: 71 72 73 74 75	1m	Do not award the mark if additional incorrect numbers are circled. Accept alternative unambiguous indications, eg ticks, crosses.
15b	 An explanation which recognises that 1003 is not a multiple of 3, eg: 'Because 1003 is not divisible by 3' 'Because 1003 is not a multiple of 3' 'Because 1003 is not in the 3 times table' 'Because 1 divided 1003 by 3 and there was a remainder' 'Because 1003 ÷ 3 has a decimal answer' 'Because 1 + 0 + 0 + 3 = 4, and 4 is not a multiple of 3' 'Because 1003 has a digital sum of 4' 'Because 1002 is the nearest in the 3 times table' 'Because 1000 is not divisible by 3' 'Because 999 is divisible by 3'. 	1m U1	No mark is awarded for circling 'No' alone. Do not accept vague or arbitrary explanations, eg: • 'Because 1003 ends in 3' • 'Because 1003 is in the third column' • 'Because if you keep going in 3s you will go past it'. If 'Yes' is circled but a correct unambiguous explanation is given, then award the mark.

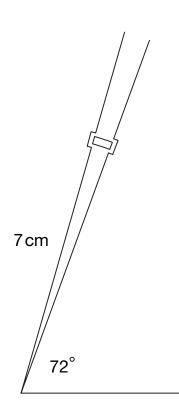
Test A questions 14–15

Test A questions 16-20

 16 Award TWO marks for three shapes drawn correctly on the diagram as shown: If the answer is incorrect, award ONE mark for: the 'L' shape and any one of the two circles drawn correctly OR both circles drawn correctly AND the 'L' shape drawn in the correct square but orientated incorrectly. 	lear.
17a 6 1m	
 An explanation which recognises that a total of 10 children read between 4 and 6 books, eg: '10 children altogether read between 4 and 6 books, and 7 + 1 makes 8, so that leaves 2 children' 'Because 7 add 1 is 8, and you need 2 more' 'Because 10 children read 4 to 6 books' '8 and 2 more make 10 children altogether' '1 + 7 = 8, 8 + 2 = 10'. 	8'
18 196.45 1 <i>m</i>	
19 Award TWO marks for the correct answer of 50 Up to $2m$ Up to $2m$ If the answer is incorrect, award ONE mark for evidence of appropriate working, eg $U1$ Calculation must be perform award of ONE mark. $15 \div 3 = 5$ $5 \times 10 =$ wrong answer $5 \times 10 =$ wrong answer $U2$	med for the
20a Answer in the range $\frac{1}{10}$ to $\frac{3}{20}$ inclusive. 1m Range includes $\frac{1}{7}$, $\frac{1}{8}$, $\frac{1}{9}$ and Accept decimals (0.1 to 0.1 or percentages (10% - 15%) 20b Answer in the range 40 to 50 inclusive. 1m	15 inclusive)

Test A question 21

Markers will use a transparent overlay of this page to mark pupils' answers to this question.



10 cm

Question	Requirement	Mark	Additional guidance
21	 Award TWO marks for a triangle drawn with an angle in the range 70° to 74° inclusive AND length of sloping line in the range 6.9 cm to 7.1 cm inclusive (ie upper vertex of triangle within inner box on diagram). If the answer is incorrect, award ONE mark for: a completed triangle drawn with an angle in the range 70° to 74° inclusive. OR a completed triangle drawn with an angle in the range 69° to 75° inclusive AND length of sloping line in the range 6.8 cm to 7.2 cm inclusive. 	Up to 2m	 Accept drawings where any side has been extended past a vertex. Accept drawings which do not use the given 10cm base line, provided they have used a line with a length in the range 9.9cm to 10.1cm inclusive. Accept for ONE mark drawings not using the given 10cm base line which have a base line outside the range 9.9cm to 10.1cm, provided they have an angle in the range 70° to 74° inclusive AND a sloping line in the range 6.9cm to 7.1cm inclusive. Accept for ONE mark drawings of incomplete triangles, provided they have an angle in the range 70° to 74° inclusive AND a sloping line in the range 6.9cm to 7.1cm inclusive.

Test A questions 22–23

Question	Requirement	Mark	Additional guidance
22	Award TWO marks for the correct answer of 53	Up to 2m	
	If the answer is incorrect, award ONE mark for evidence of appropriate		In all cases accept follow through of ONE error in working.
	working which contains no more than ONE arithmetical error, eg:		Calculation must be performed for the award of ONE mark.
	 long division algorithm wrong answer 		Do not award any marks if the final answer is missing.
	$ \begin{array}{r} 16 848 \\ 800 \\ 48 \\ -48 \\ \overline{0} \end{array} $		Variations on algorithms are acceptable, provided they represent a viable and complete method.
	 short division algorithm wrong answer 16)84⁴8 		Short division methods must be supported by evidence of appropriate carrying figures to indicate use of a division algorithm.
	 repeated addition / subtraction methods, eg 		No mark is awarded for repeated addition / subtraction the wrong number of times.
	$ \begin{array}{r} 848 \\ -400 \\ 448 \\ -400 \\ 25 \times 16 \\ -48 \\ -48 \\ 3 \times 16 \\ \hline 0 \\ \hline 0 \\ \hline 0 \\ 848 \div 2 = 424 \\ 424 \div 2 = 212 \end{array} $		No mark is awarded for repeated halving the wrong number of times.
	212 ÷ 2 = 106 106 ÷ 2 = wrong answer		
23	Award TWO marks for all three numbers, as shown: 94, 95, 96 If the answer is incorrect, award ONE mark for: • two numbers correct and none	Up to 2m U1	Accept numbers written in any order. All three numbers and no incorrect numbers must be given for the award of TWO marks.
	 incorrect OR three numbers correct and one incorrect OR 		
	93, 94, 95, 96, 97		

Question	Requirement	Mark	Additional guidance
1a	4	1m	
1b	599	1m	
2	Award TWO marks for the four lines drawn as shown: 11×11 $4 \times 5 \times 6$ greater than 100 $56 + 27 + 17$ less than 100 $335 - 745$ equal to 100 $4000 \div 50$ If the answer is incorrect, award ONE mark for three correct lines drawn AND not more than one incorrect line drawn.	Up to 2m	Do not award any marks if two or more incorrect lines are drawn. Lines need not touch the boxes provided the intention is clear.
За	5	1m	
3b	2	1m	
4	9 1 + 9 1 + 1 9 = 201 OR $9 9 + 9 1 + 1 1 = 201$	1m (U1)	Accept the three two-digit numbers written in any order.
5	125	1m	
6a	£10.51	1m	
6b	Award TWO marks for the correct answer of £2.26 If the answer is incorrect, award ONE mark for evidence of appropriate method, eg 34.99 + 12.75 = 47.74 50 - 47.74 OR 50 - 12.75 - 34.99	Up to 2m	Accept for ONE mark £226 OR £226p as evidence of appropriate method. Answer need not be obtained for the award of ONE mark.

Test B questions 1–6

Question	Requirement	Mark	Additional guidance
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		Accept alternative unambiguous indications such as Y and N .
7a	First column of table completed correctly.	1m	
7b	Second column of table completed correctly.	1m	
8a	£14.40	1m	Do not accept £14.4
8b	20	1m	Do not accept £20
9	(5, 2)	1m	Coordinates must be written in the correct order. Accept unambiguous answers written on the diagram.
10	Numbers circled as shown: 30 40 50 60 70	1m	Accept alternative unambiguous indications, eg numbers ticked, crossed or underlined.
11	Answer in the range 65 to 75 inclusive.	1m	
12	1 5 9 13	1m	

Test B questions 7–12

Test B questions 13–15

Question	Requirement	Mark	Additional guidance
13a	Any odd numbered multiple of 10, ie 10 OR 30 OR 50 OR 70 OR 90 OR any number ending with any of the pairs of digits above.	1m	
13b	 An explanation which recognises that all multiples of 20 are also multiples of 10, eg: 'Because all the numbers in the 20 times table are also in the 10 times table' 'Because all multiples of 20 are multiples of 10' 'Because 20 is in the 10 times table' 'All multiples of 20 go in box A because 10 goes into them' '20 is a multiple of both 20 and 10, and so is 40, 60, etc' 'Because if it's not a multiple of 10, it can't be a multiple of 20' 'Because if it is a multiple of 20, it has to be a multiple of 10' 	1m U1	 Do not accept vague or arbitrary explanations, eg: 'Because 40 is a multiple of 10' 'Because they would be in box A instead' 'Because all the multiples of 10 are multiples of 20' 'Because 10 is a multiple of 20'.
14	£11.25	1m	
15	Any rectangle with an area of 8 squares, eg	1m	Accept slight inaccuracies in drawing provided the intention is clear.

Question	Requirement	Mark	Additional guidance
16	Award TWO marks for four faces correctly shaded as shown:	Up to 2m U1	The width of each shaded rectangle is irrelevant provided the intention is clear.
17	Award TWO marks for the correct answer of 60 If the answer is incorrect, award ONE mark for evidence of appropriate method, eg 800 – 500 = 300 300 ÷ 5	Up to 2m U1	Answer need not be obtained for the award of ONE mark.
18a 18b	Answer in the range 3:10pm to 3:20pm inclusive. Answer in the range 13 degrees to	1m 1m	The answer is a specific time (see page 5 for guidance).
	14 degrees inclusive.		
19	Award TWO marks for the correct answer of 30 If the answer is incorrect, award ONE mark for evidence of appropriate method, eg $45 \div 3 = 15$ 15×2	Up to 2m	Answer need not be obtained for the award of ONE mark.

Test B questions 16–19

Test B questions 20–25

Question	Requirement	Mark	Additional guidance
20	Award TWO marks for all three numbers in order as shown: 129 AND 7492 AND 51 If the answer is incorrect, award ONE mark for two out of three numbers correct.	Up to 2m	Do not accept 129.0 OR 7492.0 OR 51.0 OR any other equivalent answers with zeroes after the decimal point.
21	40%	1m	Do not accept equivalent fractions or decimals.
22a	400	1m	Answer must be in grams.
22b	1200 g OR 1.2 kg OR for finding the correct difference between 1.6 kg and the answer given for 22a.	1m	Accept 1200 OR 1.2 OR 1kg 200g
23	Two numbers circled as shown: 29 39 49 59 69	1m	Do not award the mark if additional incorrect numbers are circled. Accept alternative unambiguous indications, eg numbers ticked, crossed or underlined.
24	Diagram completed as shown:	1 <i>m</i>	Accept slight inaccuracies in drawing (see page 3 for guidance).
25	Award TWO marks for the correct answer of 14 If the answer is incorrect, award ONE mark for evidence of appropriate method, eg $17.5 \times 4 = 70$ $70 \div 5$	Up to 2m U1	Accept for ONE mark 140 OR 1.4 as evidence of appropriate method. Answer need not be obtained for the award of ONE mark.

Mark scheme for the mental mathematics test

Applying the mark scheme

Please note that pupils will not be penalised if they record any information given in the question or show their working. Markers will ignore any annotation, even if in the answer space, and mark only the answer. Markers will accept an unambiguous answer written in the stimulus box, or elsewhere on the page.

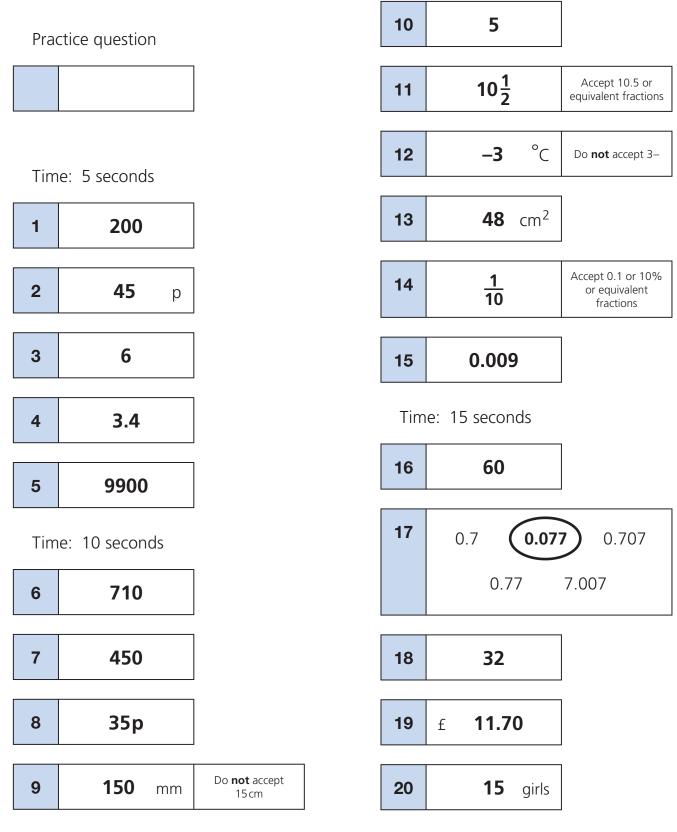
Full mark scheme information is given on page 20. In addition, a 'quick reference' mark scheme is provided on page 19. This is presented in a similar format to the pupil's answer sheet.

General guidance

The general guidance for marking the written tests also applies to marking the mental mathematics test. In addition, the following principles apply.

- 1. Unless stated otherwise in the mark scheme, accept answers written in words, or a combination of words and figures.
- 2. Where units are specified, they are given on the answer sheet. Pupils are not penalised for writing in the units again.
- 3. Where answers are required to be ringed, do not accept if more than one answer is ringed, unless it is clear which is the pupil's intended answer. Accept also any other way of indicating the correct answer, eg underlining.

Mental mathematics 2006 quick reference mark scheme



Question	Requirement	Mark	Additional guidance
1	200	1m	
2	45p	1m	
3	6	1m	
4	3.4	1m	
5	9900	1m	
6	710	1m	
7	450	1m	
8	35р	1m	
9	150mm	1m	Do not accept 15 cm
10	5	1m	
11	10 ¹ / ₂	1m	Accept 10.5 OR equivalent fractions.
12	-3°C	1m	Do not accept 3–
13	48 cm ²	1m	
14	<u>1</u> 10	1m	Accept 0.1 OR 10% OR equivalent fractions.
15	0.009	1m	
16	60	1m	
17	0.7 0.777 0.707 0.77 7.007	1m	Accept any other way of indicating the answer, eg underlining. Do not accept if more than one answer is indicated unless the pupil's intention is clear.
18	32	1m	
19	£11.70	1m	
20	15 girls	1m	

Mental mathematics questions 1–20

EARLY YEARS

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